

# First passage times reveal underlying free energy landscapes

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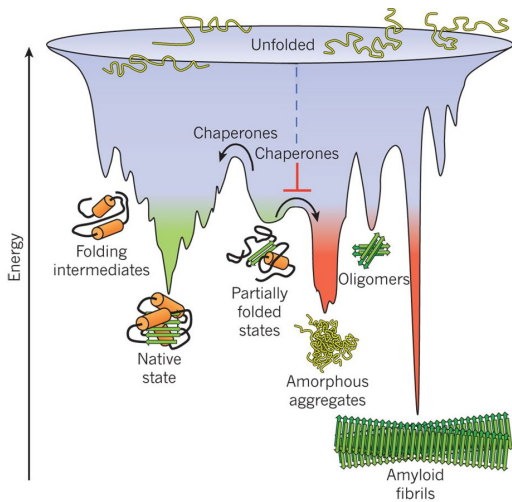
# Outline

1. Motivation: Biological membrane transport
2. Experiments: Colloidal model channel system with controlled potential landscapes
3. First passage time distributions in a colloidal system
4. First passage time distributions in molecular systems

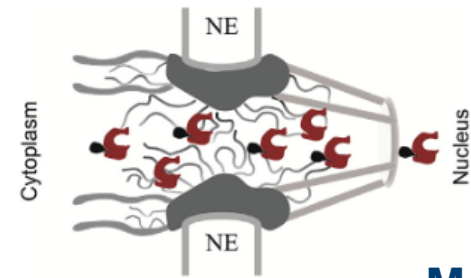
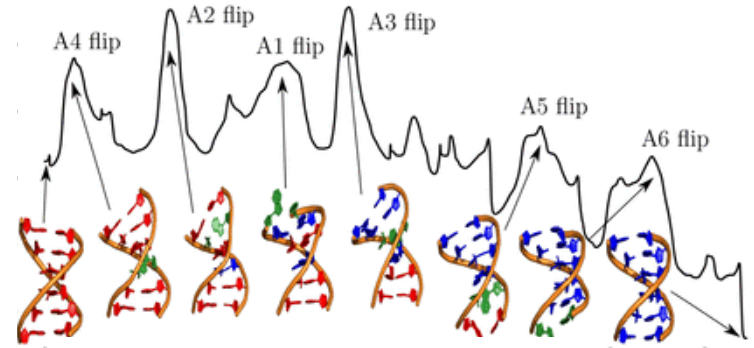
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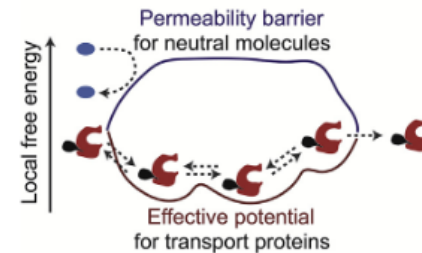
# Free-energy landscapes govern biological phenomena



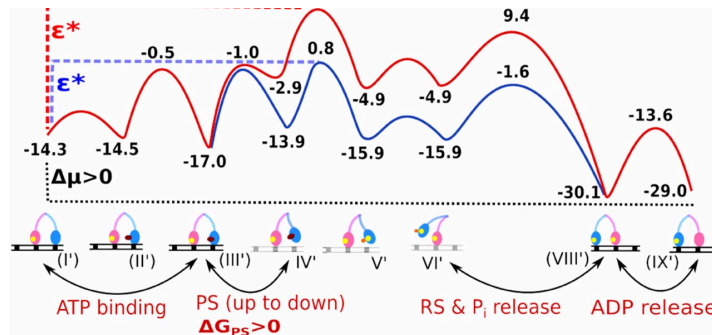
## Protein/DNA/RNA folding



## Membrane transport



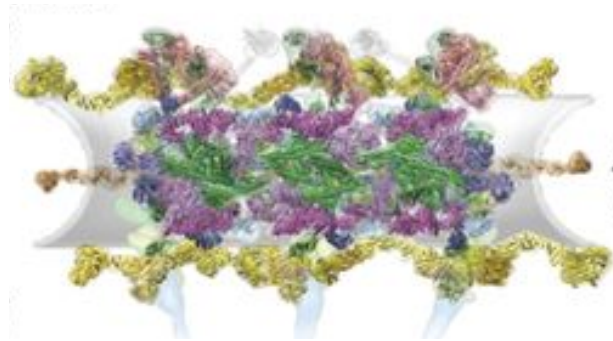
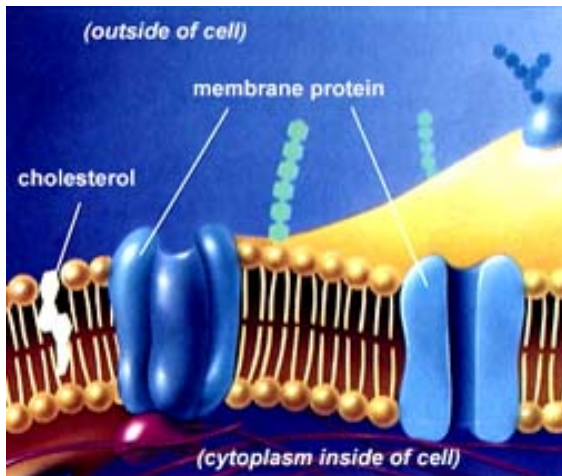
## Molecular motors



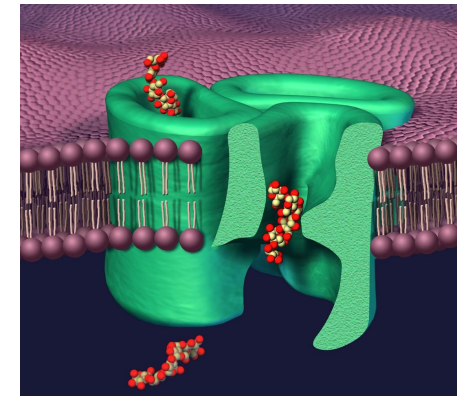


# Example: Biological membrane transport

- Efficient and selective transport through a variety of pores and channels



Nuclear pore complex  
~150 nm

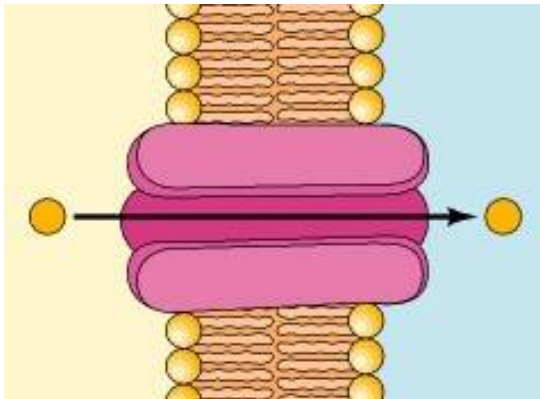


Maltoporin  
~5 nm

- Mechanism of selective transport: size, shape, specific binding...?

# Our experimental model for membrane transport

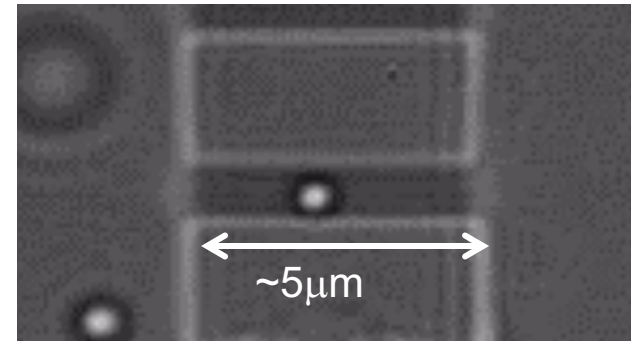
Biological channels



Length scales ~ nm  
Timescales ~ ns



**Microscale**  
Colloidal model channel



Length scales ~ μm  
Timescales ~ s

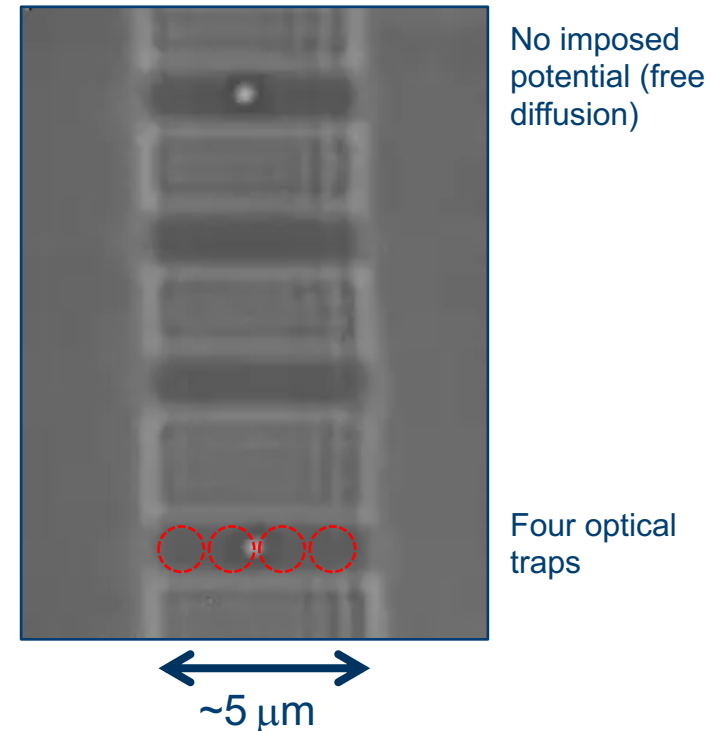
Molecular systems are difficult to visualise and directly manipulate...  
...so consider a colloidal model system that is more experimentally accessible

# Colloidal system offers full control over all key parameters

**Experimental approach:**  
colloids + microfluidics +  
optical tweezers

- Controlled channel **structure**
- Controlled **interactions**
- Resolved transport **dynamics**

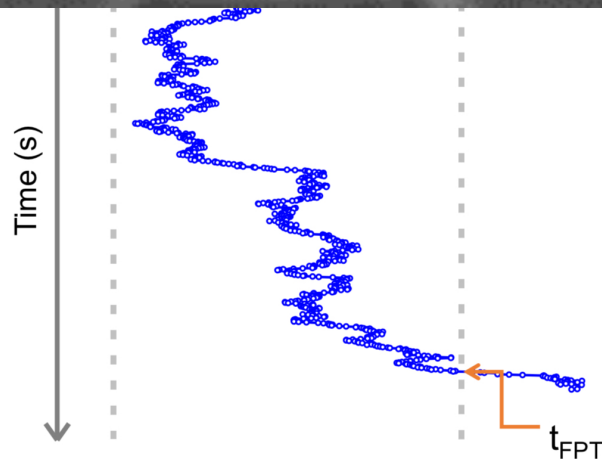
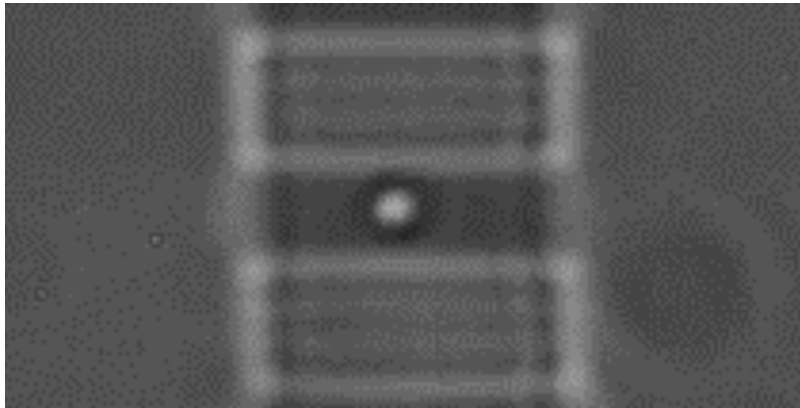
→ Explore links between structure/interactions and dynamics



# Outline

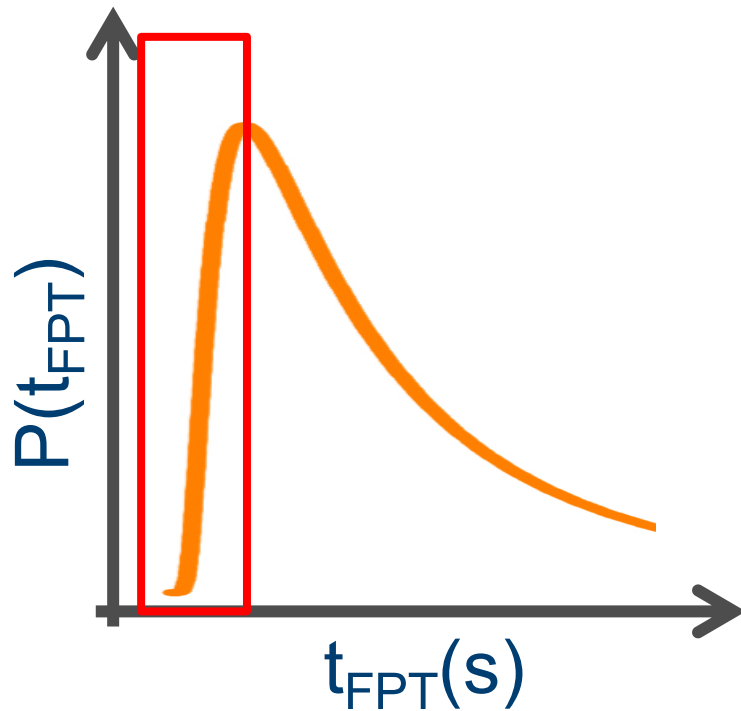
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# First passage times are easy to observe with colloids



- **First passage time** = time it takes for a process to attain a certain value *for the first time* i.e. how long does it take a particle to exit a channel

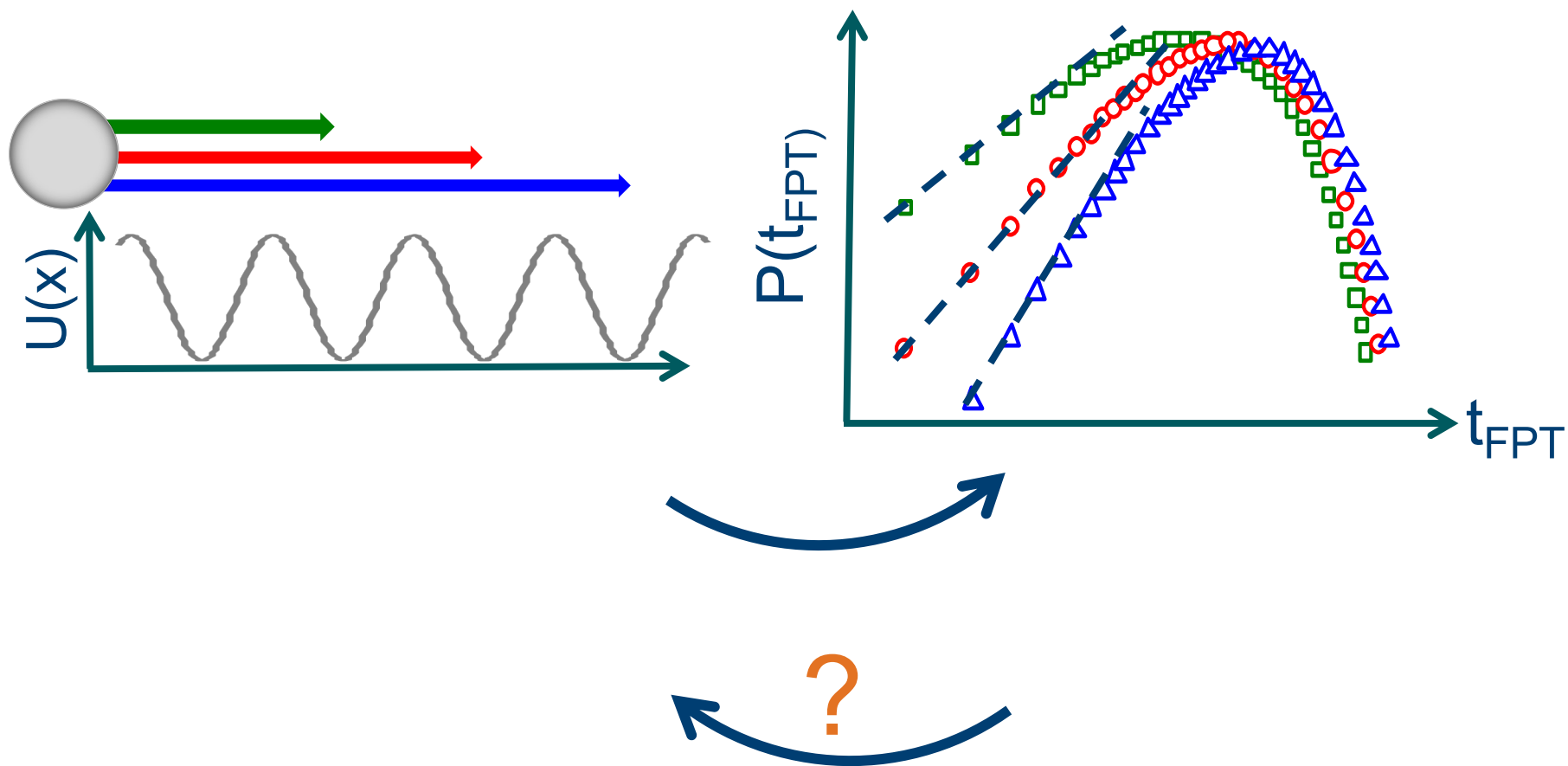
# Full first passage time distributions can be measured



**Probability distribution of first passage times,  $P(t_{\text{FPT}})$**  = probability an event will happen for the first time after a certain elapsed time

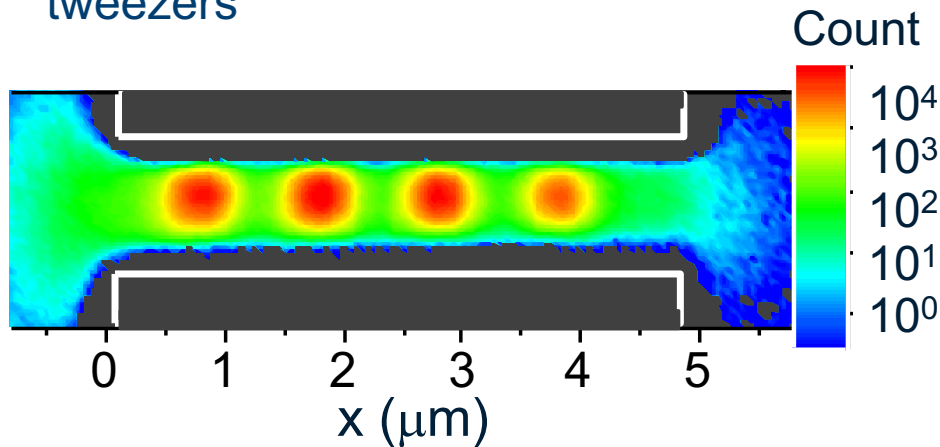
**Crucially,**  
 $P(t_{\text{FPT}})$  sensitively linked to underlying free energy landscape

# Does the shape of the first passage time distribution reveal details of the potential landscape?

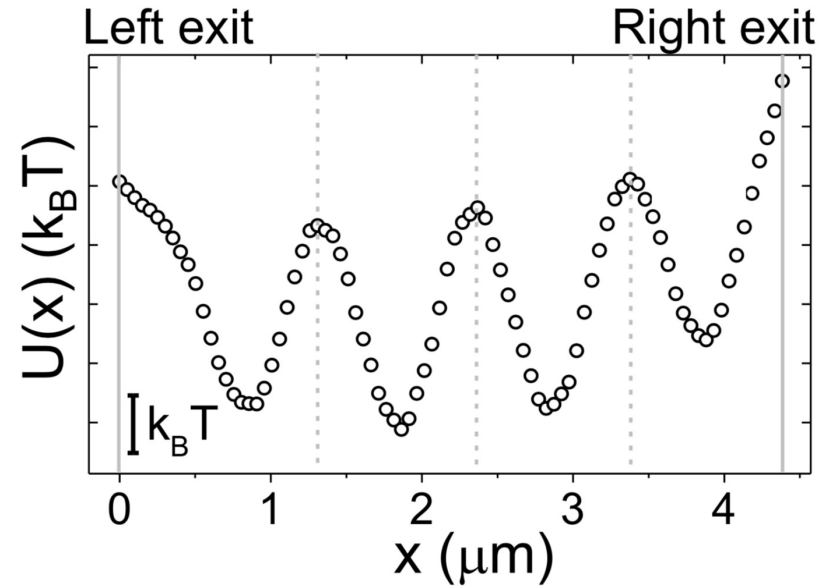


# Model channel system with four states

Potential landscapes with multiple minima imposed with optical tweezers



2D histogram of particle positions



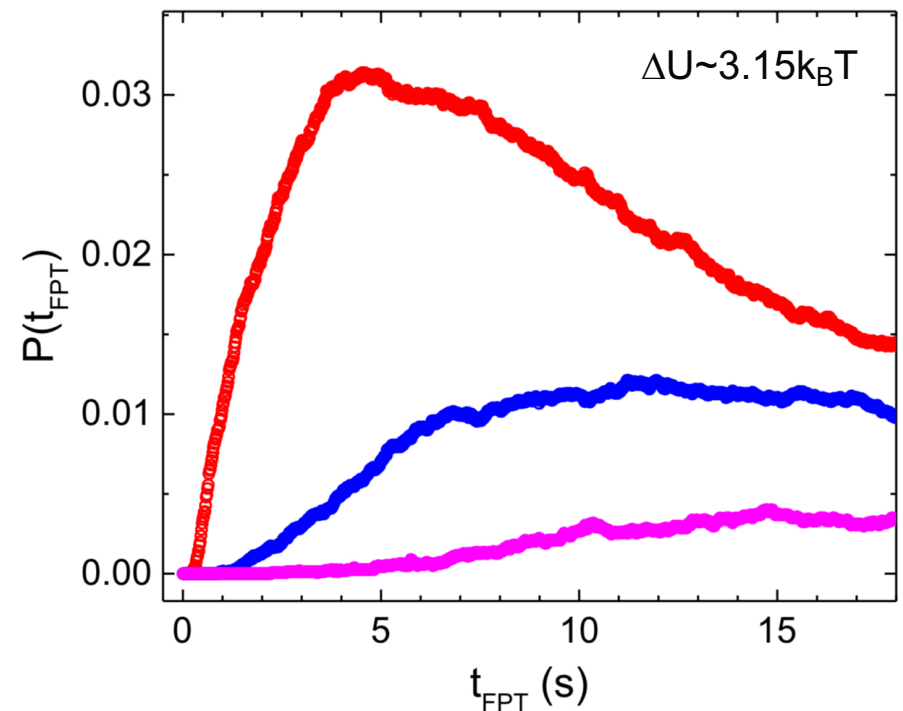
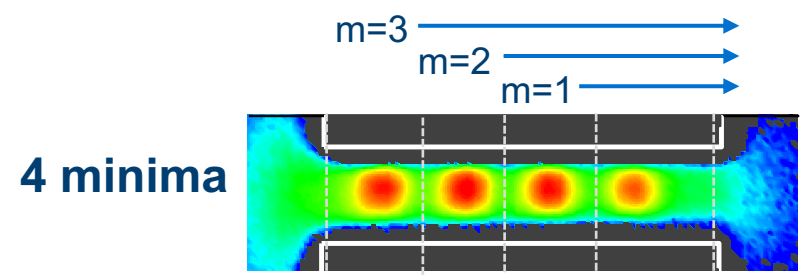
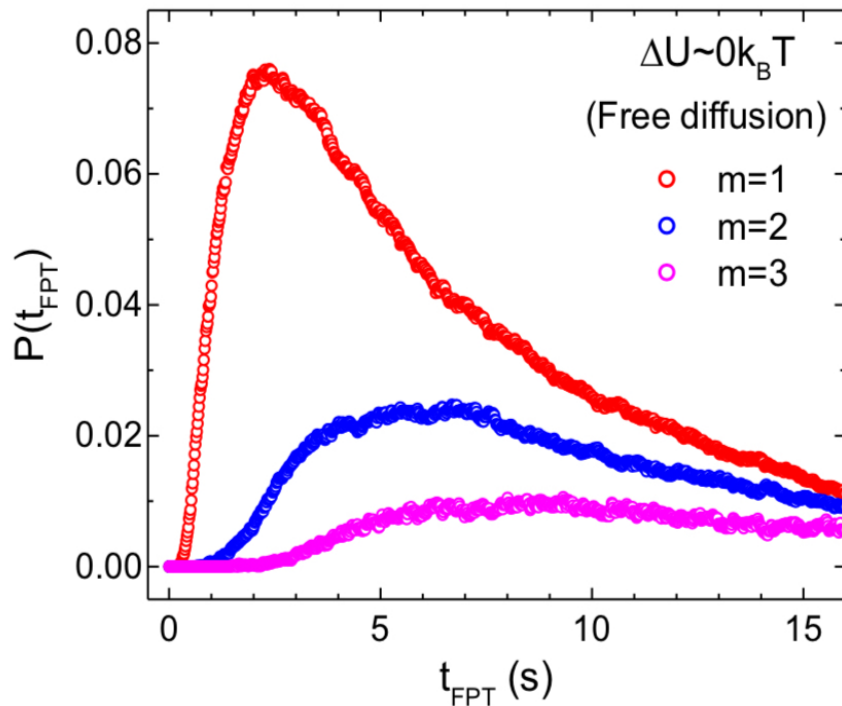
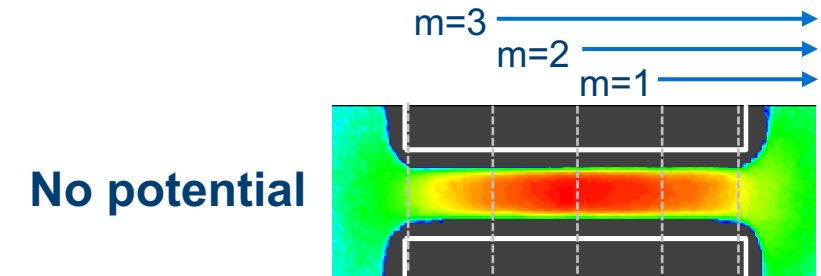
Potential landscape,

$$U(x) \sim -\ln(P(x))$$

with  $P(x)$  the probability distribution of particle positions

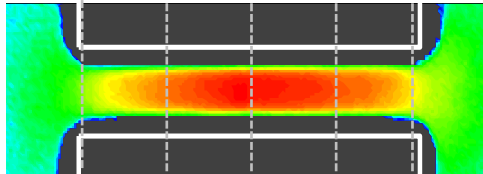


# First passage distributions on a linear scale appear similar...

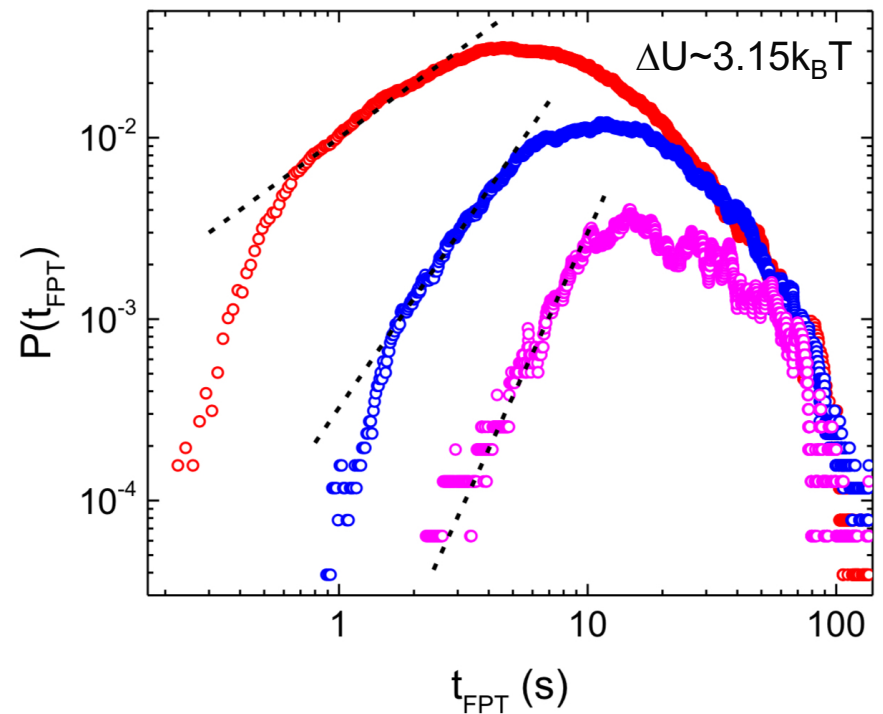
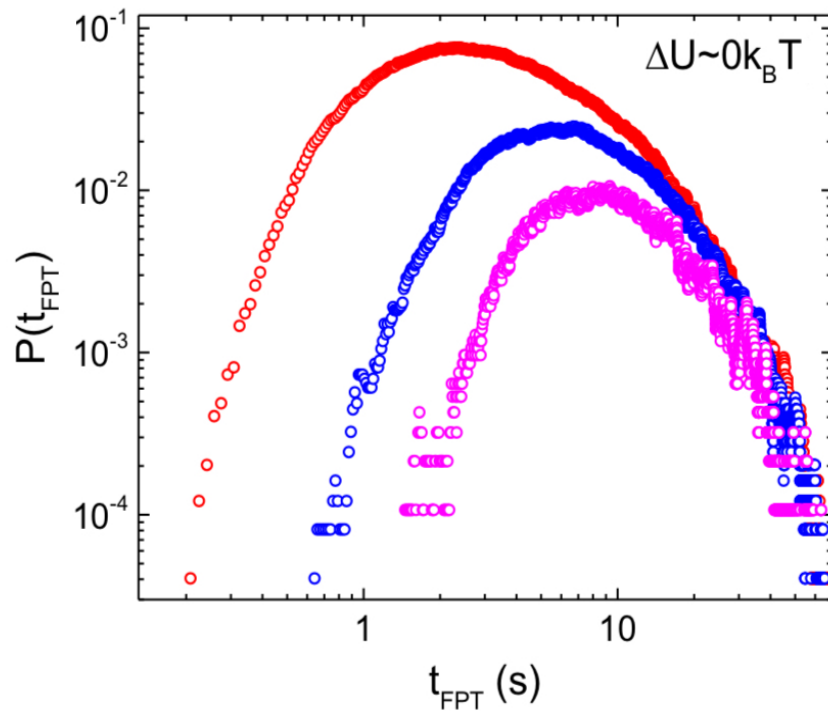
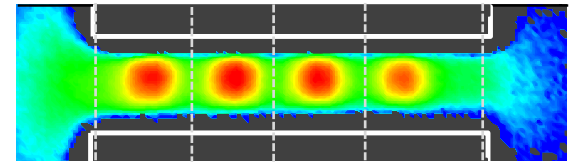


# ...but potential minima qualitatively change distributions

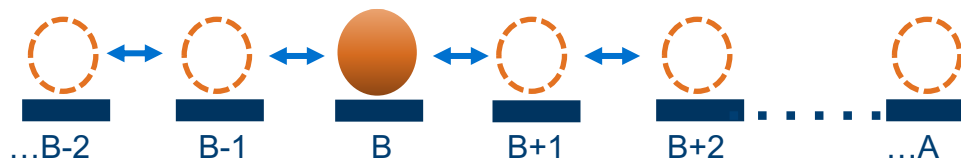
No potential



4 minima

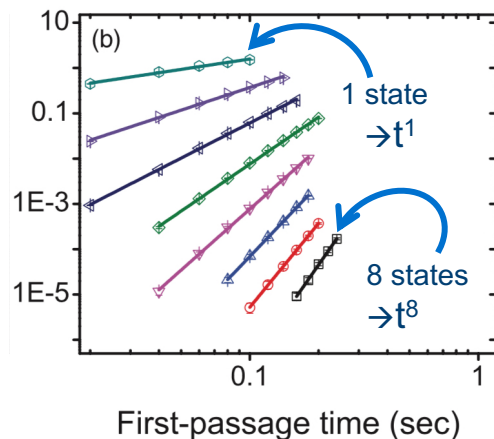


# First passage time distributions in a 1D network



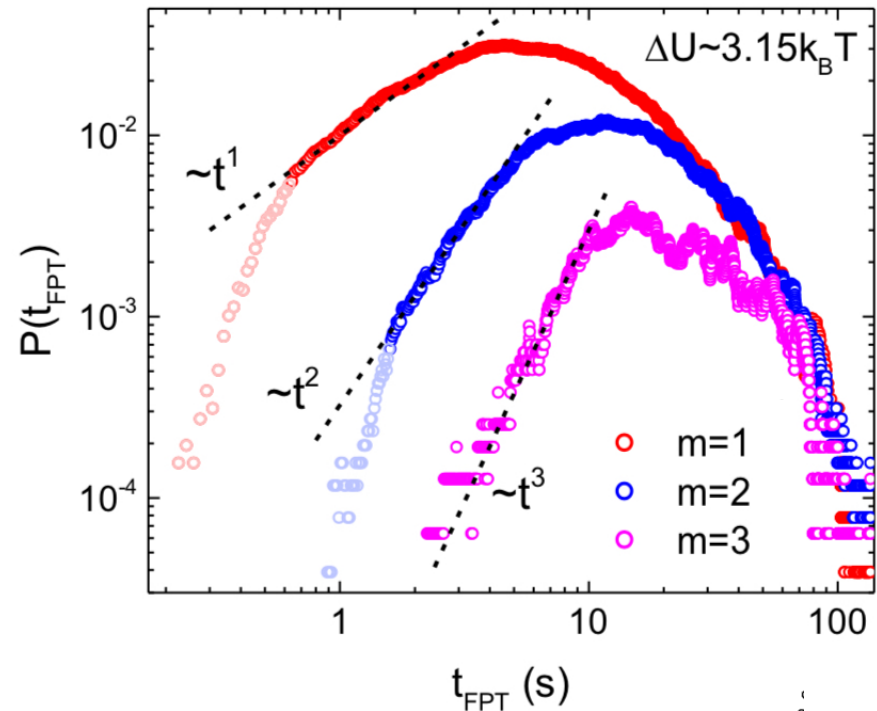
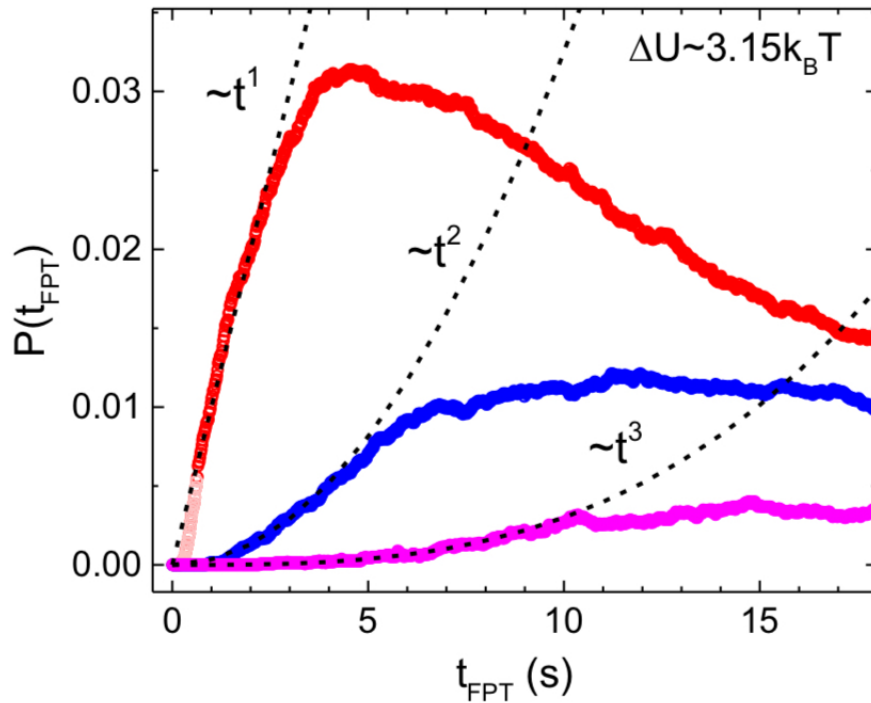
Short-time regime:  $\ln P(t_{FPT}) \simeq (A - B - 1) \ln t + C$

Simulation results:

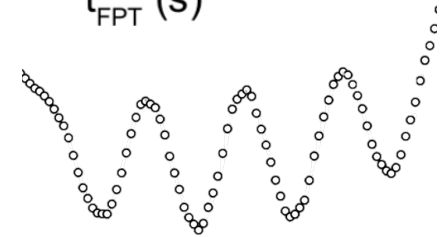


Measurement of  $P(t_{FPT})$  at short times  $\rightarrow$  number of states that must be crossed to exit

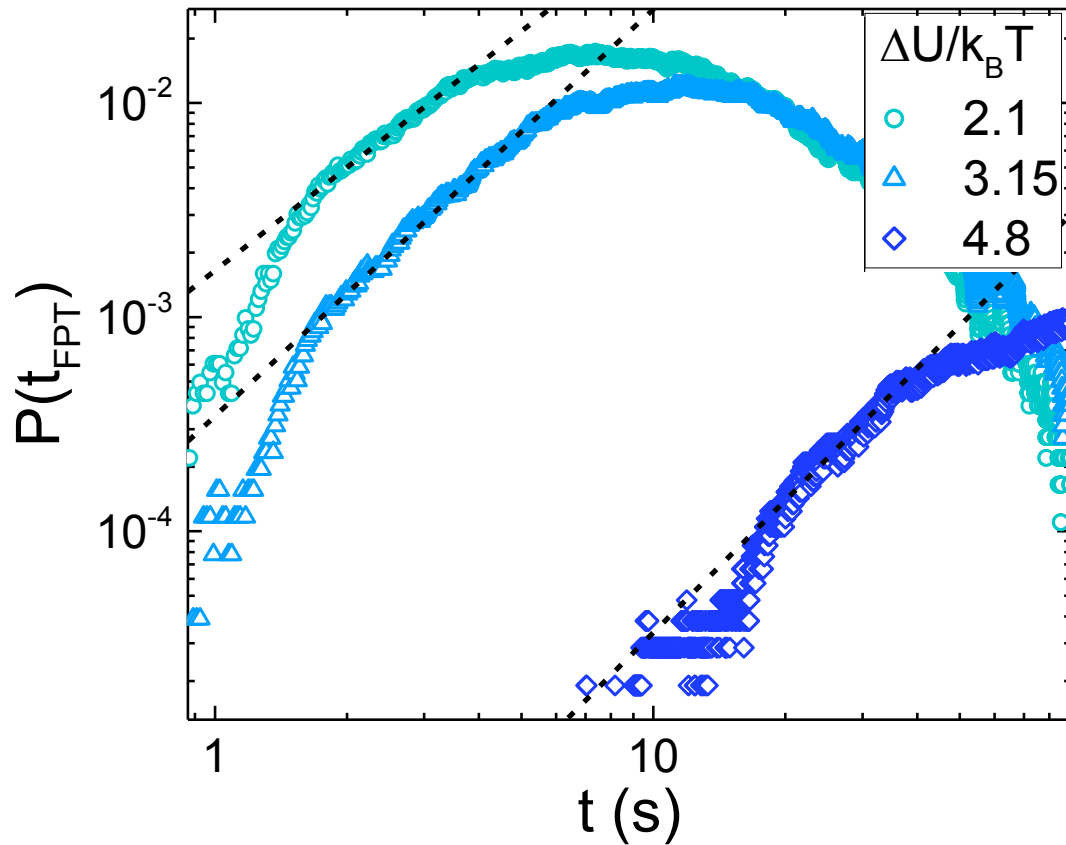
# Short-time regime reflects number of potential minima



Distributions exhibit a short-time power law regime with  $P(t_{\text{FPT}}) \sim t^m$  scaling consistent with theory

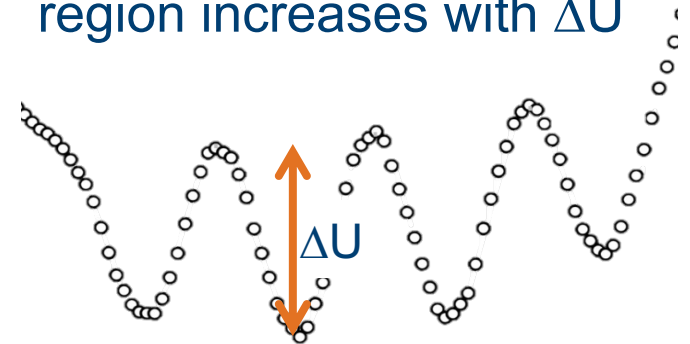


# Length of power law regime increases with $\Delta U$

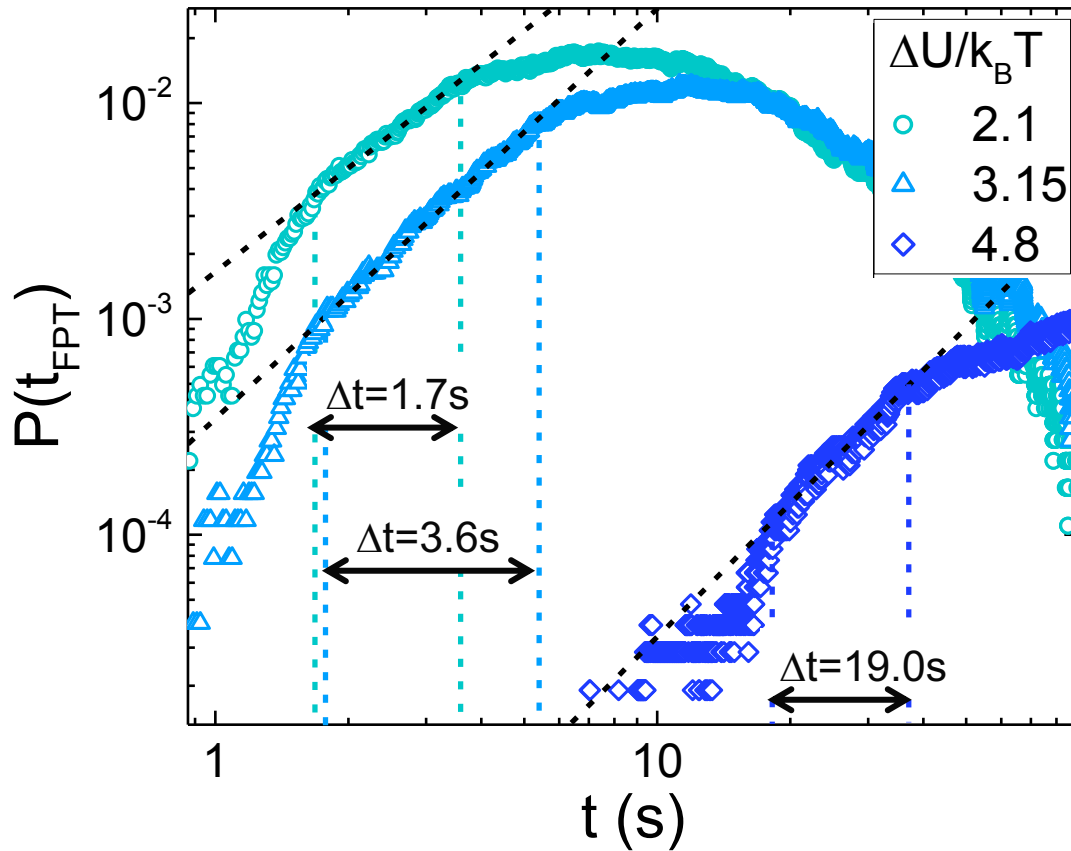


Short-time regime for  $m=2$  distributions

- All distributions exhibit a power-law regime,  $t^m$ , with  $m \sim 2$
- Length of power-law (linear) region increases with  $\Delta U$

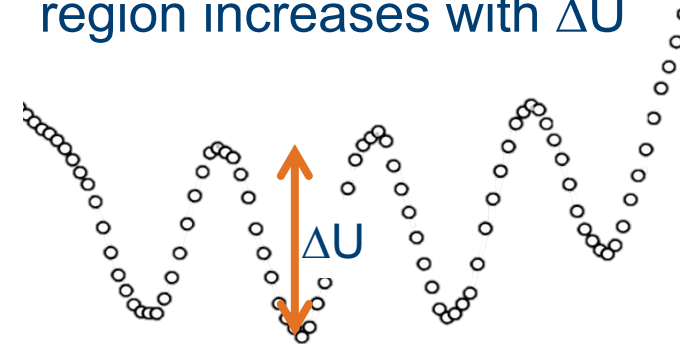


# Length of power law regime increases with $\Delta U$

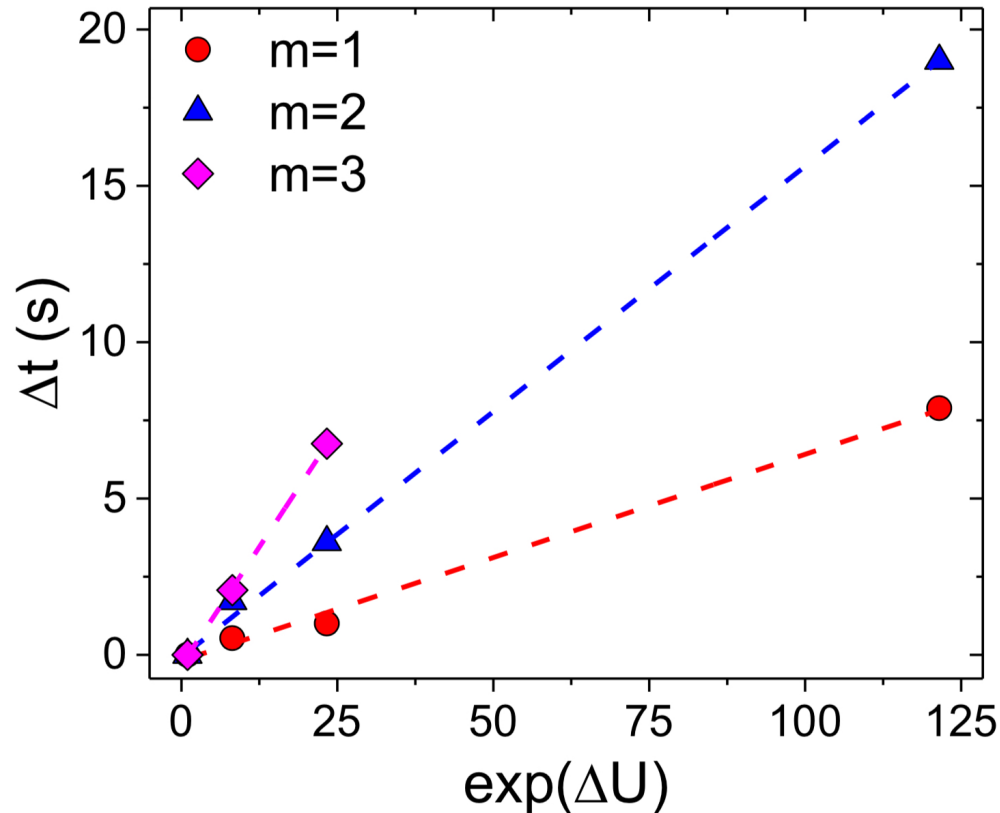


Short-time regime for  $m=2$  distributions

- All distributions exhibit a power-law regime,  $t^m$ , with  $m \sim 2$
- Length of power-law (linear) region increases with  $\Delta U$



# Length of power law regime scales linearly with $\Delta U$



Length of power law regime scales with potential depth

→ Residence time important

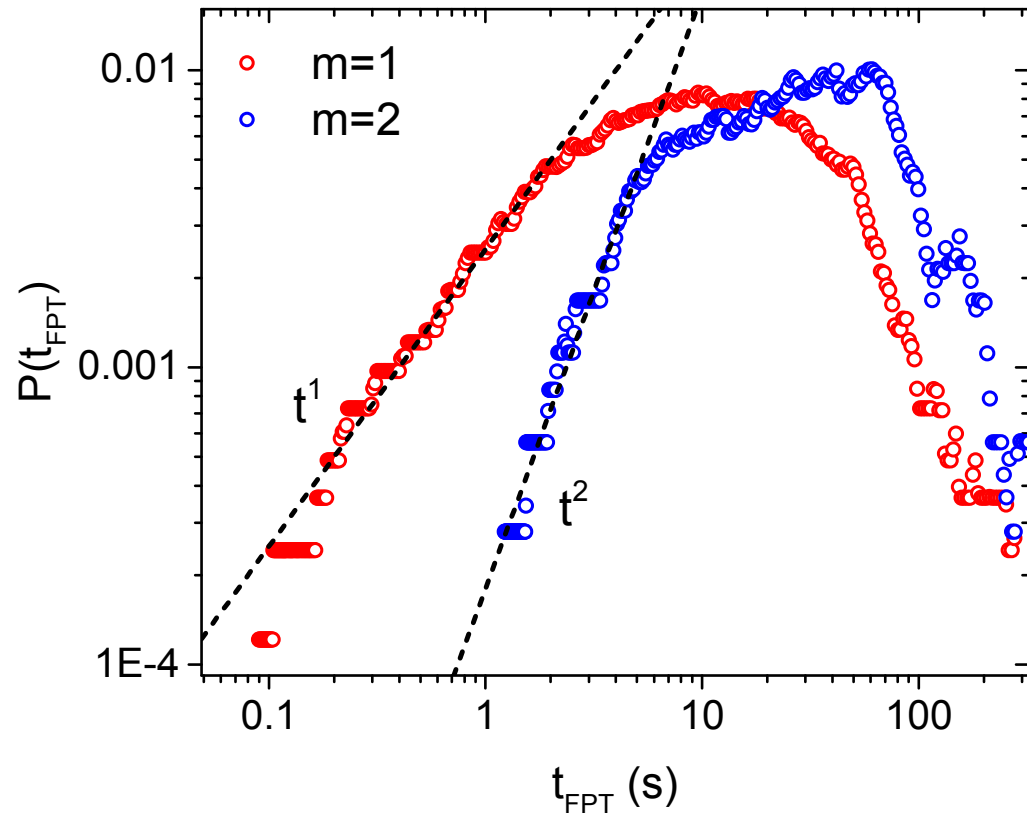
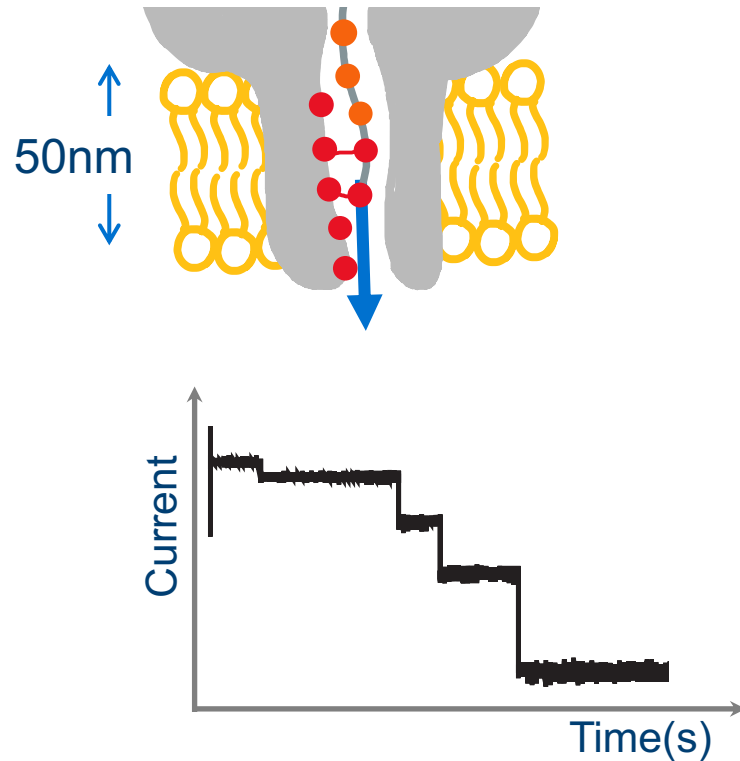
→ Route to infer potential depth

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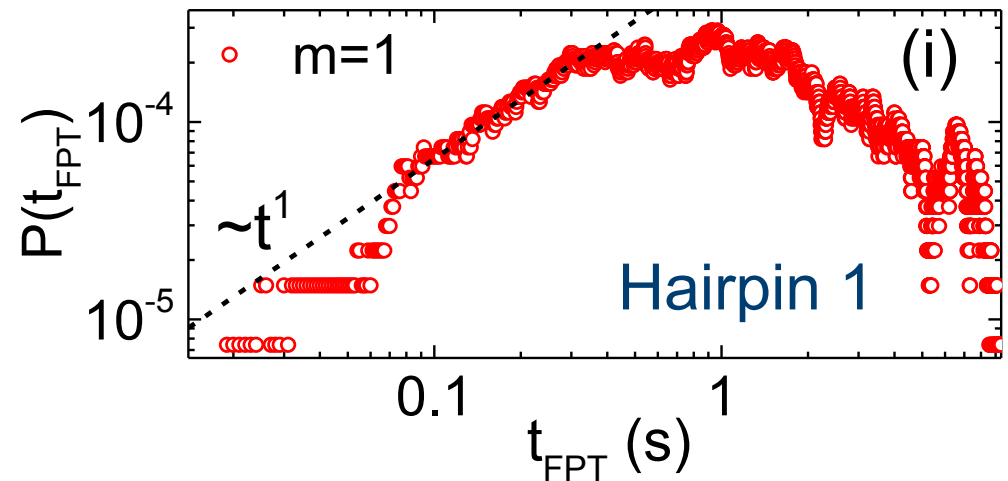
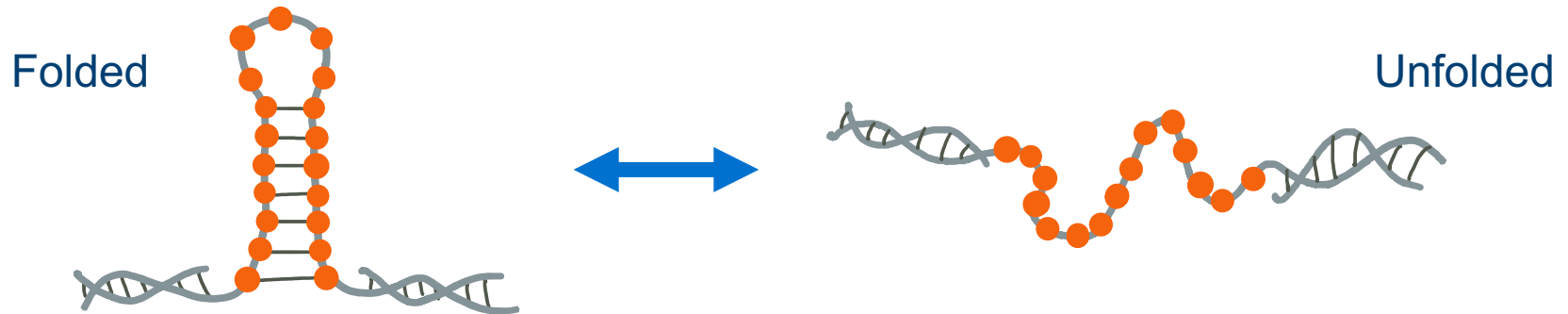
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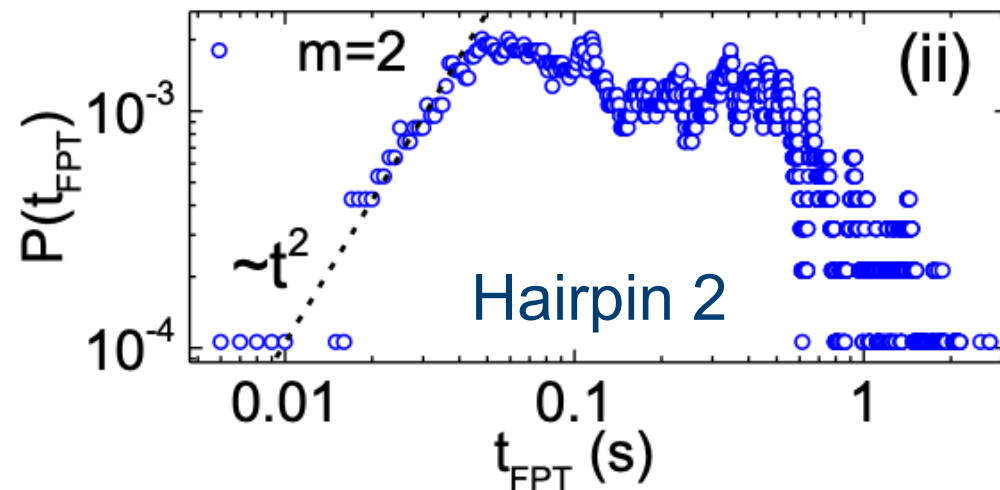
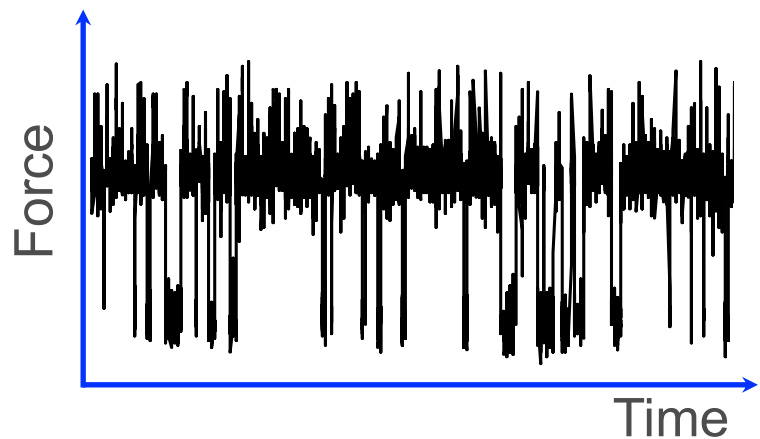
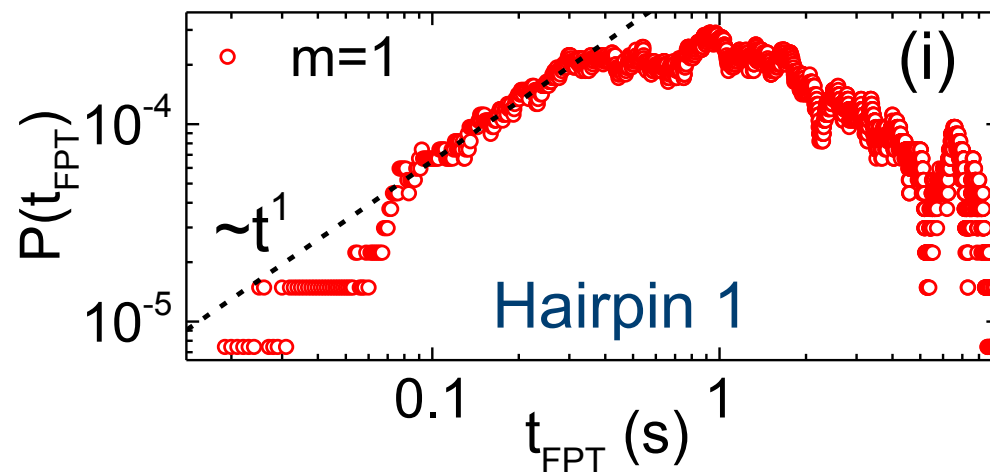
# Molecular example 1: biological pore transport



# Molecular example 2: (un)folding of a DNA hairpin

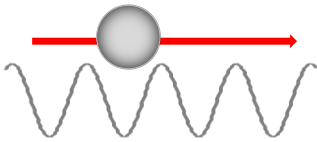


# Molecular example 2: (un)folding of a DNA hairpin

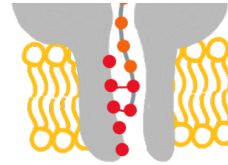


# Universal behaviour of the FPT distribution

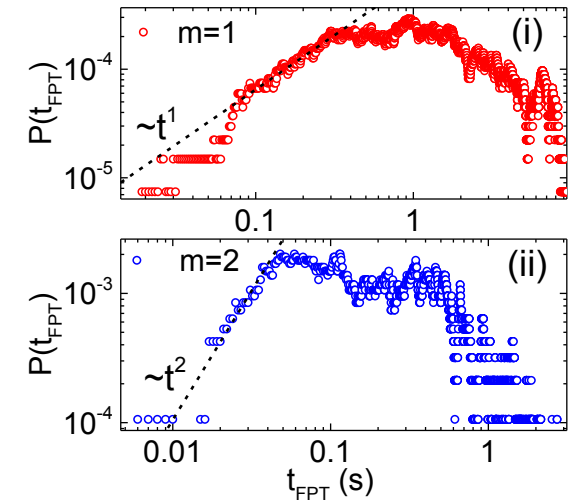
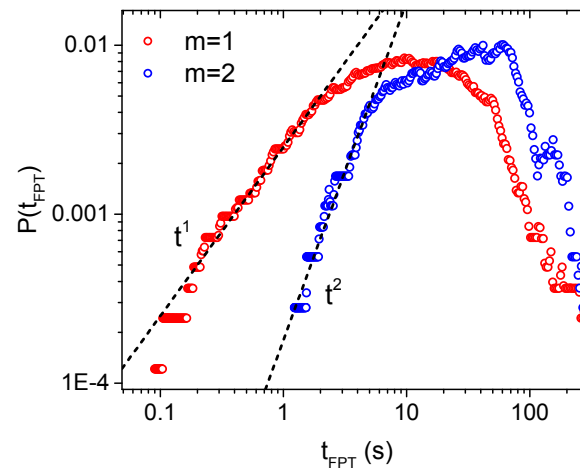
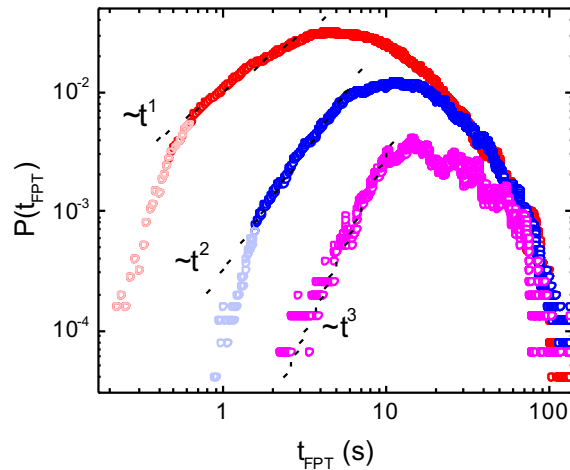
Colloidal  
channel



Biological  
pore



DNA  
Hairpin



Mesoscale

Microscale

# Acknowledgements

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